

St Andrew's CE Primary School

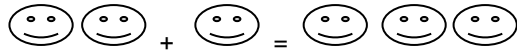


**Whole School Written Calculation Policy
Pencil and paper procedures
Key Stages 1 and 2**

Addition

Year 1

Counting on using objects and numicon



Also using numicon

+ = signs and missing numbers

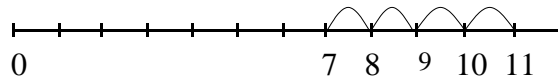
$$\begin{array}{ll} 3 + 4 = \square & \square = 3 + 4 \\ 3 + \square = 7 & 7 = \square + 4 \\ \square + 4 = 7 & 7 = 3 + \square \\ \square + \nabla = 7 & 7 = \square + \nabla \end{array}$$

Promoting covering up of operations and numbers.

Number lines

(Teacher model number lines with missing numbers)

$$7 + 4 = 11$$



Partition into tens and ones and recombine (Spring/Summer Term)

$$\begin{aligned} 12 + 23 &= 10 + 2 + 20 + 3 \\ &= 30 + 5 \\ &= 35 \end{aligned}$$

Year 2

+ = signs and missing numbers

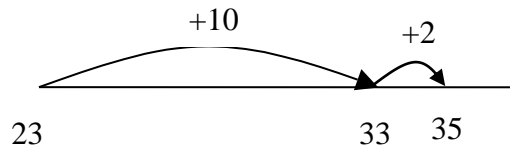
Continue using a range of equations as in Year 1 but with appropriate, larger numbers.

Extend to

$$\begin{aligned} 14 + 5 &= 10 + \square \\ \text{and adding three numbers} \\ 32 + \square + \square &= 100 \quad 35 = 1 + \square + 5 \end{aligned}$$

Refine to partitioning the second number only into tens and ones: (Autumn Term)

$$\begin{aligned} 23 + 12 &= 23 + 10 + 2 \\ &= 33 + 2 \\ &= 35 \end{aligned}$$



Partition into tens and ones and recombine (Spring & Summer Term)

Partition both numbers and recombine

$$\begin{aligned} 36 + 53 &= \\ 30 + 6 & \\ \underline{50 + 3} & \\ \underline{80 + 9} &= 89 \end{aligned}$$

Teach all three partitioning methods but this is the preferred style to adopt.

$$\begin{aligned} 24 + 17 & \\ 20 + 10 &= 30 \\ 4 + 7 &= \underline{11} \quad \text{Preferred version} \\ & \quad \underline{41} \end{aligned}$$

Mental Method – ongoing (Use a visual image)

Add 9 or 11 by adding 10 and adjusting by 1
35 + 9 = 44

Year 3

+ = signs and missing numbers

Continue using a range of equations as in Year 1 and 2 but with appropriate, larger numbers

balanced equations

$$10 + 5 = 20 - \square$$

Continue as in Year 2 but with appropriate numbers
e.g. 35 + 19 is the same as 35 + 20 – 1

Pencil and paper procedures (Autumn Term)

$$36 + 53 =$$

$$\begin{array}{r} 36 \\ +53 \\ \hline 9 \\ \underline{80} \\ 89 \end{array}$$

Pencil and paper procedures (Spring Term)

$$358 + 73 = 431$$

$$\begin{array}{r} 358 \\ + 73 \\ \hline 11 \\ 120 \\ \underline{300} \\ 431 \end{array}$$

Pencil and paper procedures – compact method (Summer Term)

$$\begin{array}{r} 36 \\ +53 \\ \hline 89 \end{array}$$

Add a near multiple of 10 to a two-digit number (Use a visual image) Mental Method – ongoing (Use a visual image)

Add 19/29 etc or 11/21 etc by adding 10/20 etc and adjusting by 1
35 + 9 = 44
35 + 19 = 54

Addition

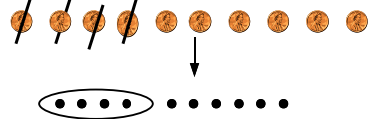
Year 4	Year 5	Year 6
<p><u>+ = signs and missing numbers</u></p> <p>Continue using a range of equations but with appropriate, larger numbers</p> <p><u>balanced equations</u></p> $6 \times 5 = \square + 15$ <p><u>Pencil and paper procedures</u> Compact method, showing numbers carried underneath</p> $\begin{array}{r} 358 \\ + 73 \\ \hline 431 \\ 11 \end{array}$ <p><u>Pencil and paper procedures</u> <u>(Summer Term)</u></p> <p>Extend to numbers with at least four digits and decimals (money context)</p> $3587 + 675 = 4262$ $\begin{array}{r} 3587 \\ + 675 \\ \hline 4262 \\ 111 \end{array}$	<p><u>+ = signs and missing numbers</u></p> <p>Continue using a range of equations but with appropriate, larger numbers</p> <p><u>balanced equations</u></p> $8 \times 6 = n + 23$ <p><u>Pencil and paper procedures</u> <u>(All Terms)</u></p> <p>Extend to numbers with at least four digits</p> $3587 + 675 = 4262$ $\begin{array}{r} 3587 \\ + 675 \\ \hline 4262 \\ 111 \end{array}$ <p>Extend to decimals (same number of decimals places) and adding several numbers (with different numbers of digits).</p> $124.90 \quad \textit{add in a zero to keep the place value}$ $\begin{array}{r} 124.90 \\ + 117.25 \\ \hline 242.15 \\ 11 \end{array}$	<p><u>+ = signs and missing numbers</u></p> <p>Continue using a range of equations but with appropriate, larger numbers</p> <p><u>balanced equations</u></p> $n \times 6 = n + 23$ <p><u>Pencil and paper procedures</u> <u>(All Terms)</u></p> <p>Extend to numbers with at least four digits</p> $63527 + 73984$ $\begin{array}{r} 63527 \\ + 73984 \\ \hline 137511 \\ 111 \end{array}$ <p>Extend to numbers with any number of digits and decimals with 1 and 2 decimal places.</p> $124.9 + 117.25 = 242.15$ $7124.90 \quad \textit{add in a zero to keep the place value}$ $\begin{array}{r} 7124.90 \\ + 1117.25 \\ \hline 8242.15 \\ 11 \end{array}$

Subtraction

Year 1

Pictures / marks/objects/numicon

Sam spent 4p. What was his change from 10p?

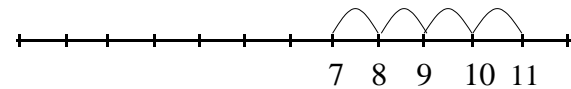


- = signs and missing numbers

$$\begin{array}{ll} 7 - 3 = \square & \square = 7 - 3 \\ 7 - \square = 4 & 4 = \square - 3 \\ \square - 3 = 4 & 4 = 7 - \square \\ \square - \nabla = 4 & 4 = \square - \nabla \end{array}$$

The difference between 7 and 11
(Counting back/taking away)

To reinforce concept. Practical strategies essential to see 'difference'.



Recording by - drawing jumps on prepared lines
- constructing own lines

(Teachers model jottings appropriate for larger numbers)

Year 2

- = signs and missing numbers

Continue using a range of equations as in Year 1 but with appropriate numbers.

Extend to $14 + 5 = 20 - \square$

Mental Method

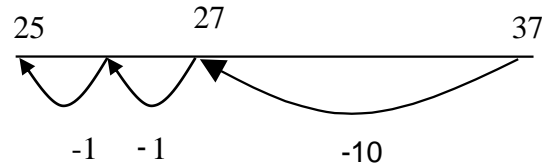
Subtract 9 or 11. Begin to add/subtract 19 or 21

$$35 - 9 = 26$$

To be taught using a 100 square

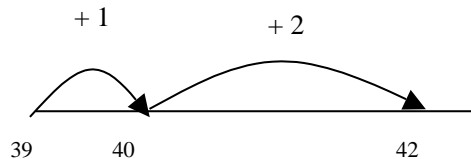
Use known number facts and place value to subtract (partition second number only) (Autumn & Spring Term)

$$\begin{aligned} 37 - 12 &= 37 - 10 - 2 \\ &= 27 - 2 \\ &= 25 \end{aligned}$$



Find a small difference by counting up

$$42 - 39 = 3$$



Summer Term

Unit digits do not cross tens boundaries (without decomposition)

$$58 - 24$$

$$50 - 20 = 30$$

$$8 - 4 = 4$$

$$\underline{34}$$

$$42 - 27$$

$$30 - 20 = 10$$

$$12 - 7 = 5$$

$$\underline{15}$$

Year 3

- = signs and missing numbers

Continue using a range of equations as in Year 2 but with appropriate numbers.

Extend to $26 + 43 = 82 - \square$

Find a small difference by counting up

Continue as in Year 2 but with appropriate numbers e.g. $102 - 97 = 5$

Mental Method

Subtract 9 or 11. Add/subtract 19 or 21

$$35 - 9 = 26$$

Use known number facts and place value to subtract Pencil and paper procedures (Autumn & Spring Terms)

Unit digits do not cross tens boundaries (without decomposition)

$$98$$

$$- 37$$

$$1 \text{ (8-7)}$$

$$\underline{60 \text{ (90-30)}}$$

$$\underline{61}$$

$$197$$

$$- 15$$

$$2$$

$$80$$

$$\underline{100}$$

$$\underline{182}$$

(Summer Term) crossing 10's boundaries

$$92 - 38 = 54$$

$$92$$

$$\underline{-38}$$

$$90 + 2 \rightarrow 80 + 12$$

$$\underline{30 + 8} \quad - \quad \underline{30 + 8}$$

$$50 + 4$$

Subtraction

Year 4

- = signs and missing numbers

Continue using a range of equations as in Year 3 but with appropriate numbers.

Extend to $126 + 43 = 200 - \square$

Mental Method

Subtract 9 or 11. Add/subtract 19 or 21 with confidence

Use known number facts and place value to subtract

Pencil and paper procedure:

(All Terms) Use decomposition

$$\begin{array}{r} \overset{8}{9} \overset{1}{2} \\ - 38 \\ \hline 54 \end{array}$$

Extend using larger numbers and decimal numbers

Year 5

- = signs and missing numbers

Continue using a range of equations as in Year 4 but with appropriate numbers.

Extend to $186 + 137 = 420 - \square$

Pencil and paper procedures

(All Terms)

$$\begin{array}{r} \overset{2}{3} \overset{4}{5} \overset{1}{2} \\ - 178 \\ \hline 174 \end{array}$$

Extend using larger numbers and decimal numbers

Year 6

- = signs and missing numbers

Continue using a range of equations as in Year 5 but with appropriate numbers.

Extend to $387 + 469 = 1200 - \square$

Pencil and paper procedures

(All Terms)

$$\begin{array}{r} \overset{2}{3} \overset{4}{5} \overset{1}{2} \\ - 178 \\ \hline 174 \end{array}$$

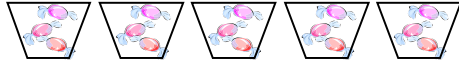
Extend using larger numbers and decimal numbers

Multiplication

Year 1

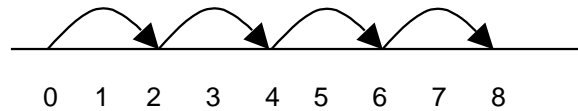
Pictures and symbols/objects/numicon

There are 3 sweets in one bag.
How many sweets are there in 5 bags?



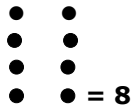
(Recording on a number line modelled by the teacher when solving problems)

4x2 (4 lots of 2)



Arrays (Spring Term)

4 lots of 2



Times Tables

Square numbers 2,5,10, doubles and halves to ten.

Year 2

x = signs and missing numbers

$$7 \times 2 = \square \quad \square = 2 \times 7$$

$$7 \times \square = 14 \quad 14 = \square \times 7$$

$$\square \times 2 = 14 \quad 14 = 2 \times \square$$

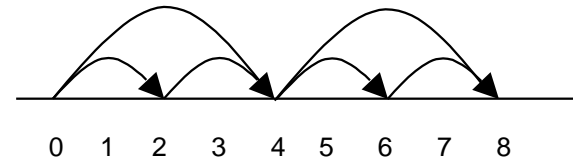
$$\square \times \nabla = 14 \quad 14 = \square \times \nabla$$

Autumn & Spring Terms

Arrays and repeated addition

2 x 4

or repeated addition
2 + 2 + 2 + 2



Mental Method

Doubling multiples of 5 up to 60

$$15 \times 2 = 30$$

Partition
(10 x 2) + (5 x 2)

$$20 + 10 = 30$$

Summer Term

$$35 \times 2 = 70$$

Partition

	T	O
x	30	5
2	60	10

Times Tables

Square numbers
2,5,10,
multiplication and
division facts, odd
and even numbers

Year 3

x = signs and missing numbers

Continue using a range of equations as in Year 2 but with appropriate numbers.

Autumn & Spring Terms

Grid method

TU x U

23 x 7 is approximately 20 x 10 = 200

$$23 \times 7 = 161$$

	T	U	
x	20	3	140
7	140	21	+ 21
			161

Summer Term

Compact method TO X O

Estimate and check

23 x 7 is approximately 20 x 10 = 200

$$23 \times 7 = 161$$

	23
x	7
	161
	2

Times Tables

Square numbers
3,4,8
multiplication
and division
facts.

Multiplication

Year 4

x = signs and missing numbers

Continue using a range of equations as in Year 3 but with appropriate numbers

Pencil and paper procedures (Autumn & Spring Terms)

HTO x O - **Short Multiplication**

Estimate and check

23 x 7 is approximately 20 x 10 = 200

23 x 7 = 161

$$\begin{array}{r} 23 \\ \times 7 \\ \hline 1561 \\ \small{1 \ 2} \end{array}$$

TO x TO & HTO x TO - **Long Multiplication expanded**
123x53=

$$\begin{array}{r} \text{HTO} \\ 123 \\ \times 53 \\ \hline 9 \\ 60 \\ 300 \\ 150 \\ 1000 \\ \hline 5000 \\ 6519 \\ \hline 1 \end{array}$$

Summer Term – compact method

$$\begin{array}{r} \text{HTO} \\ 123 \\ \times 53 \\ \hline 369 \\ 6150 \\ \hline 11 \\ 6519 \\ \hline 1 \end{array}$$

Times Tables

Square numbers
All tables to 12x
multiplication and
division facts.

Year 5

x = signs and missing numbers

Continue using a range of equations as in Year 4 but with appropriate numbers

Estimate and check

1125 x 7 is approximately 1000 x 7 = 7000

Pencil and paper procedures – compact method (All Terms)

1125 x 7 = 7875

This method to be used when multiplying by 1 digit

$$\begin{array}{r} 1125 \\ \times 7 \\ \hline 7875 \\ \small{1 \ 3} \end{array}$$

Extend using larger numbers and decimals

Pencil and paper procedures –long multiplication (All Terms)

Estimate and check

$$\begin{array}{r} 2372 \\ \times 78 \\ \hline 18976 \\ \small{251} \\ \hline 166040 \\ \small{251} \\ \hline 185016 \\ \small{111} \end{array}$$

Extend using larger numbers and decimals

Times Tables

Square numbers
All tables to 12x
multiplication and
division facts.

Year 6

x = signs and missing numbers

Continue using a range of equations as in Year 5 but with appropriate numbers

4987 x 8 = 39896

Continue with the compact method when multiplying by 1 digit

Pencil and paper procedures –compact method multiplication (All Terms)

Estimate and check

$$\begin{array}{r} 2372 \\ \times 78 \\ \hline 18976 \\ \small{251} \\ \hline 166040 \\ \small{251} \\ \hline 185016 \\ \small{111} \end{array}$$

Pencil and paper procedures –compact method multiplication (All Terms)

Estimate and check

7.2 x 3.8 is approximately 7 x 4 = 28

$$\begin{array}{r} 7.2 \times 3.8 \\ \text{U. } \frac{1}{10} \frac{1}{100} \\ 7.2 \end{array}$$

$$\begin{array}{r} \times 3.8 \\ 5.76 \\ 21.60 \\ \hline 27.36 \\ \small{1} \end{array}$$

Times Tables

Square numbers
All tables to 12x
multiplication and
division facts.

Division

Year 1

Pictures / marks

9 children get into teams of 3 to play a game.
How many teams are there? (Grouping)



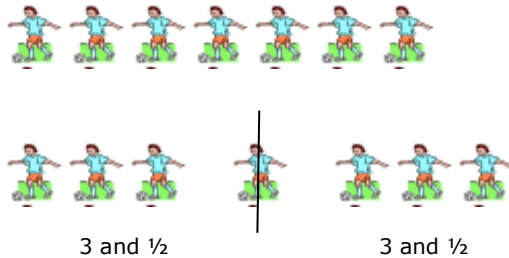
Finding 1/2 and 1/4

Using objects/numicon to find 1/2 and 1/4 of numbers practically.

1/2 of odd numbers

(Spring)

Using objects to find 1/2 of odd numbers



Year 2

÷ = signs and missing numbers

$$6 \div 2 = \square \qquad \square = 6 \div 2$$

$$6 \div \square = 3 \qquad 3 = 6 \div \square$$

$$\square \div 2 = 3 \qquad 3 = \square \div 2$$

$$\square \div \nabla = 3 \qquad 3 = \square \div \nabla$$

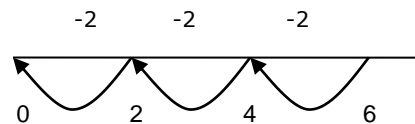
Understand division as sharing and grouping

Sharing – 6 sweets are shared between 2 people. How many do they have each?

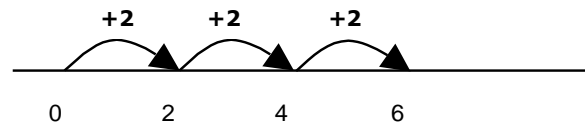


6 ÷ 2 can be modelled as:

Grouping – There are 6 sweets. How many people can have 2 each? (repeated subtraction)



(How many 2's make 6?) Counting on in 2s to make 6.



Year 3

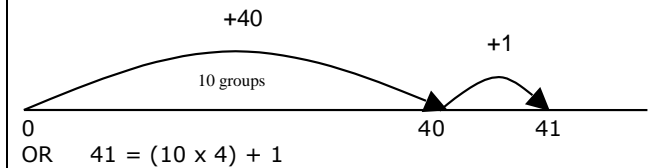
÷ = signs and missing numbers

Continue using a range of equations as in Year 2 but with appropriate numbers.

Understand division as sharing and grouping (Autumn Term)

Remainders

41 ÷ 4 = 10 r1



Spring Term - Chunking method

$$56 \div 4 = 14$$

$$\begin{array}{r} -40 (10 \times 4) \\ 16 \\ -16 (4 \times 4) \\ \hline 0 \end{array}$$

Summer Term - Bus stop method (with no remainders)

$$\begin{array}{r} 14 \\ 4 \overline{) 56} \\ \underline{4} \\ 16 \\ \underline{16} \\ 0 \end{array}$$

Division

Year 4

÷ = signs and missing numbers

Continue using a range of equations as in Year 3 but with appropriate numbers.

Pencil and paper procedures – Bus stop method – short division (All Terms)

146 ÷ 8 is approximately 150 ÷ 10 = 15

$$\begin{array}{r} 018r2 \\ 8 \overline{)146} \end{array}$$

Extend by dividing by 7 and 9 and begin to show remainders as simple fractions e.g. $\frac{2}{8}$ is $\frac{1}{4}$

Pencil and paper procedures - (Spring & Summer Term)

Using chunking method for division for long division

552 ÷ 24 = 23

$$\begin{array}{r} 23 \\ 24 \overline{)552} \\ \underline{-480} \quad (20 \times 24) \\ 72 \quad (3 \times 24) \end{array}$$

Year 5

÷ = signs and missing numbers

Continue using a range of equations as in Year 4 but with appropriate numbers.

Pencil and paper procedures - Compact Method (Autumn/Spring Term)

146 ÷ 8 is approximately 150 ÷ 10 = 15

This method to be used when multiplying by 1 digit

$$\begin{array}{r} 018r2 \\ 8 \overline{)146} \end{array}$$

With Remainders

Pencil and paper procedures – (Summer Term)

$$\begin{array}{r} 018r\frac{1}{4} \text{ (or .25)} \\ 8 \overline{)146} \end{array}$$

Remainders

Return to chunking method for division by 2 digit numbers

Quotients expressed as fractions or decimal fractions
61 ÷ 4 = 15 $\frac{1}{4}$ or 15.25

$$\begin{array}{r} 23r\frac{1}{3} \\ 24 \overline{)560} \\ \underline{-480} \quad (20 \times 24) \\ 80 \\ \underline{-72} \quad (3 \times 24) \\ 8 \end{array}$$

Year 6

÷ = signs and missing numbers

Continue using a range of equations as in Year 5 but with appropriate numbers.

Continue with pencil and paper procedures for Year 5

Remainders

Quotients expressed as fractions or decimal fractions

$$676 \div 8 = 84.5$$

Pencil and paper procedures

977 ÷ 36 is approximately 1000 ÷ 40 = 25

Using chunking for division of larger number and dividing by 2-digit numbers as Year 5